

# FORMULAS : Economics

Marginal Revenue =  $\frac{\Delta TR}{\Delta Q}$

• For perfect comp  
MR = AR = P

• For imperfect comp

MR =  $\frac{\Delta TR}{\Delta Q} = \frac{P \Delta Q + Q \Delta P}{\Delta Q}$

• Marginal Cost =  $\frac{\text{Labor rate}}{\text{Marg. Prod}}$

• Avg. var. Cost =  $\frac{\text{Total var. cost}}{Q} = \frac{w}{Q}$

• MR =  $P \left(1 - \frac{1}{E}\right)$   
own price elasticity!

own price elasticity =  $\frac{\% \text{ change in quantity demanded}}{\% \text{ change in own price}} = \frac{\Delta Q}{\Delta P} \cdot \frac{P_0}{Q_0}$

income elasticity =  $\frac{\% \text{ change in quantity demanded}}{\% \text{ change in income}}$   
Normal goods  $\rightarrow +ve \rightarrow P \downarrow \rightarrow Q \uparrow$   
Inferior  $\rightarrow -ve \rightarrow P \downarrow \rightarrow Q \downarrow$

cross price elasticity =  $\frac{\% \text{ change in quantity demanded}}{\% \text{ change in price of related good}}$   
Substitute  $\rightarrow +ve \rightarrow P \uparrow \rightarrow Q \uparrow$   
Complement  $\rightarrow -ve$

breakeven points:

perfect competition: AR = ATC

imperfect competition: TR = TC

short-run shutdown points:

perfect competition: AR < AVC

imperfect competition: TR < TVC

Profit Maximized when  
MR = MC & MC is rising  
OR TR - TC max

nominal GDP<sub>t</sub> for year t =  $\sum_{i=1}^N P_{i,t} Q_{i,t}$   $\rightarrow$  Current price  
=  $\sum_{i=1}^N (\text{price of good } i \text{ in year } t) \times (\text{quantity of good } i \text{ produced in year } t)$

real GDP for year t =  $\sum_{i=1}^N P_{i, \text{base year}} Q_{i,t}$   $\rightarrow$  Base price

• Quantity theory of money

$MV = PY$

M ~ Money supply  
Y ~ Expenditure (also inc)  
 $\frac{M}{P}$  ~ Real money supply

=  $\sum_{i=1}^N (\text{price of good } i \text{ in base year}) \times (\text{quantity of good } i \text{ produced in year } t)$

GDP deflator for year t =  $\frac{\text{Nominal GDP}}{\text{Real GDP}} \times 100$   
=  $\frac{\sum_{i=1}^N P_{i,t} Q_{i,t}}{\sum_{i=1}^N P_{i, \text{base year}} Q_{i,t}} \times 100 = \frac{\text{nominal GDP in year } t}{\text{value of year } t \text{ output at base year prices}} \times 100$

• Demand  $\propto$  Income  $\propto \frac{1}{\text{Int. rates}}$

GDP, expenditure approach:

GDP = C + I + G + (X - M)  
where:  
C = consumption spending  
I = business investment (capital equipment, inventories)  
G = government purchases  
X = exports  
M = imports

$(S - I) = (G - T) + (X - M)$

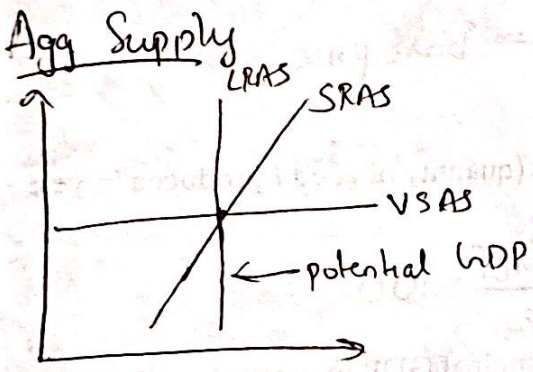
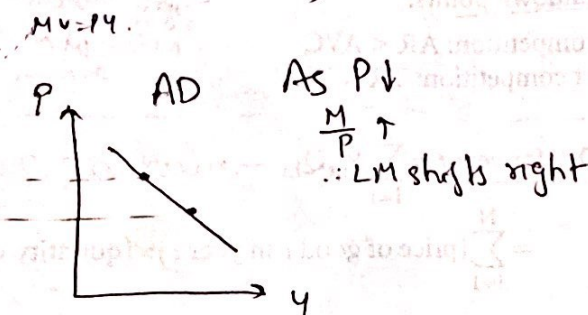
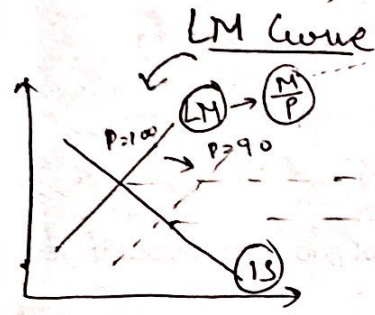
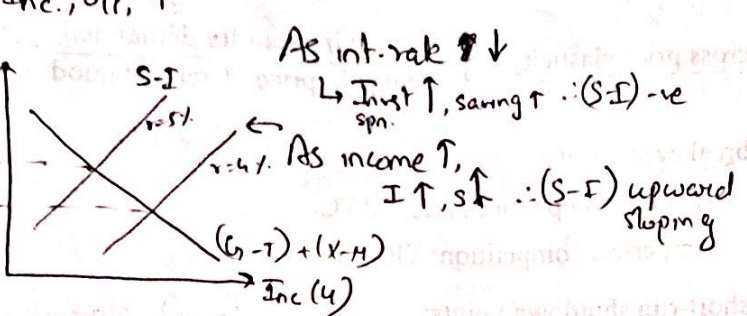
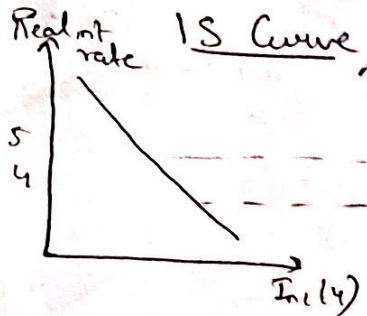
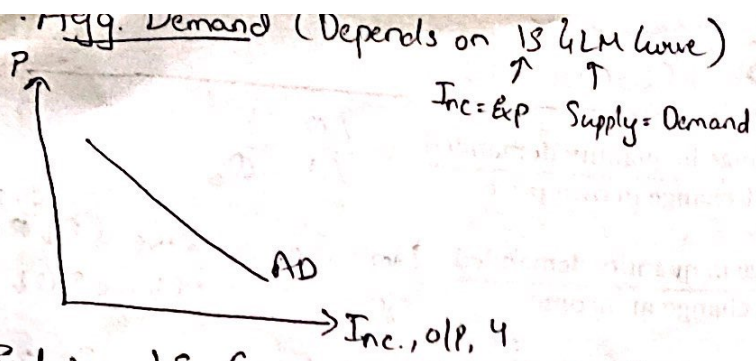
Participation Ratio =  $\frac{\text{No. of ppl in labour force}}{\text{Total pop. of working age people}}$

• Unemployment rate =  $\frac{\text{Unemployed}}{\text{Labor force}}$

• Labor force = Working + Looking for job

FORMULAS

approach:  
 national income  
 income = compensation  
 + corporate and govt  
 + interest income  
 + unincorporated  
 income



M = imports  
 X = exports  
 G = government purchase  
 I = business investment  
 C = consumption

approach:

national income + capital consumption allowance + statistical discrepancy

- national income = compensation of employees (wages and benefits)
- + corporate and government enterprise profits before taxes
- + interest income
- + unincorporated business net income (business owners' incomes)
- + rent
- + indirect business taxes - subsidies (taxes and subsidies that are included in final prices)

- personal income = national income
- + transfer payments to households
- indirect business taxes
- corporate income taxes
- undistributed corporate profits

personal disposable income = personal income - personal taxes

growth in potential GDP = growth in technology +  $W_L$ (growth in labor) +  $W_C$ (growth in capital)

where:

- $W_L$  = labor's percentage share of national income
- $W_C$  = capital's percentage share of national income

growth in per-capita potential GDP = growth in technology +  $W_C$ (growth in the capital-to-labor ratio)

where:

$W_C$  = capital's percentage share of national income

consumer price index =  $\frac{\text{cost of basket at current prices}}{\text{cost of basket at base period prices}} \times 100$

money multiplier =  $\frac{1}{\text{reserve requirement}}$  \* Money Created =  $\frac{\text{New Deposit}}{\text{Reserve Req.}}$

equation of exchange: money supply  $\times$  velocity = price  $\times$  real output (MV = PY)

Fisher effect: nominal interest rate = real interest rate + expected inflation rate

neutral interest rate = real trend rate of economic growth + inflation target

Demand for money  $\propto \frac{1}{\text{int. rate}}$   $\propto$  Income

\* fiscal multiplier:

When  $G \uparrow$ ,  $Y \uparrow$ ? how much

$$\frac{1}{1 - MPC(1 - t)}$$

where:

$t$  = tax rate

$MPC$  = marginal propensity to consume

consumption  
disposable inc

(20)

$$* \text{ real exchange rate} = \frac{\text{nominal exchange rate}}{\text{spot rate}} \times \left( \frac{\text{CPI}_{\text{base currency}}}{\text{CPI}_{\text{price currency}}} \right)$$

$$\frac{1 \text{ USD} = 2 \text{ EUR} = 2 \text{ USD}}{\text{EUR}} \quad \text{real exchange rate} = \frac{\text{nominal exchange rate}}{\left( \frac{\text{CPI}_{\text{price currency}}}{\text{CPI}_{\text{base currency}}} \right)}$$

forward premium (+) or discount (-) for the base currency:

$$\frac{\text{forward}}{\text{spot}} - 1$$

• Multiply int. rates by  $\frac{x}{360}$  if fwd contract is for  $x$  days

\* interest rate parity:

$$\frac{\text{forward}}{\text{spot}} \frac{(1 + \text{interest rate}_{\text{price currency}})}{(1 + \text{interest rate}_{\text{base currency}})}$$

by  $x \cdot (1 + \text{rate})^{x/360}$

\* Marshall-Lerner condition:

If  $W_X \epsilon_X + W_M (\epsilon_M - 1) > 0$ , currency depr will  $\uparrow (X - M)$   
 $\downarrow$  trade def.

where:

$W_M$  = proportion of trade that is imports

$W_X$  = proportion of trade that is exports

$\epsilon_M$  = elasticity of demand for imports

$\epsilon_X$  = elasticity of demand for exports

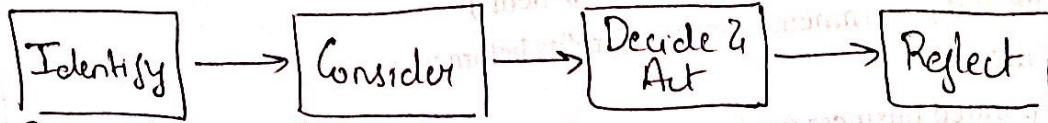
(19)  $GNP = GDP - \text{Inc of foreigners} + \text{Inc of citizens in for. country}$

• Terms of Trade =  $\frac{\text{Price of Export}}{\text{Price of Import}}$

• Current Acct = Pvt Saving + Govt Saving - Invest

# Ethics

## Ethical decision making framework



- Relevant facts
  - Conflict of int
  - Ethical princ
  - Stakeholders owed
- Situational influences
  - Additional guidance
  - Alternative act

## Standards of Professional Conduct

### Professionalism

- ↳ Knowledge of laws
- ↳ Independence & Objectivity
- ↳ Misrepresentation
- ↳ Misconduct

### Duties to Employer

- ↳ Loyalty
- ↳ Additional compensation arrangements
- ↳ Respect of supervisor

### Resp. as CFAI member

- ↳ Conduct as participants in program
- ↳ Ref. to CFAI designat

### Integrity of Capital MKT

- ↳ Material non-public info
- ↳ MKT manipulation

### Invest analy, research

- ↳ Comm w/ clients & prosp. clients
- ↳ Diligence & reasonable basis
- ↳ Record retention

### Duties to clients

- ↳ Loyalty, Prudence & Care
- ↳ Fair dealing
- ↳ Suitability
- ↳ Perf. presentation
- ↳ Preservation of confidential info

### Conflict of interest

- ↳ Disclosure of conflicts
- ↳ Priority of trans
- ↳ Referral fees

# MULAS

$$= CF_0 + \frac{CF_1}{(1+k)^1} + \frac{CF_2}{(1+k)^2} + \dots + \frac{CF_n}{(1+k)^n} = \sum_{t=0}^n \frac{CF_t}{(1+k)^t}$$

$$IRR: 0 = CF_0 + \frac{CF_1}{(1+IRR)^1} + \frac{CF_2}{(1+IRR)^2} + \dots + \frac{CF_n}{(1+IRR)^n} = \sum_{t=0}^n \frac{CF_t}{(1+IRR)^t}$$

If int rate +ve  
 ↳ Disc Payback > Payback  
 Rate @ which both mutually exclusive proj's NPV are equal is called crossover

payback period = full years until recovery +  $\frac{\text{unrecovered cost at the beginning of the last year}}{\text{cash flow during the last year}}$

$$PI = \frac{\text{PV of future cash flows}}{CF_0} = 1 + \frac{NPV}{CF_0}$$

Profitability index > 1 → Invest  
 < 1 → Don't

WACC =  $(w_d)[k_d(1-t)] + (w_{ps})(k_{ps}) + (w_{ce})(k_{ce})$   
 ↳ cost of Cap/Marg. cost of Cap  
 after-tax cost of debt =  $k_d(1-t)$

$$E(r) > CAPM$$

↳ Undervalued

cost of preferred stock =  $k_{ps} = D_{ps} / P$

cost of common equity:

$$k_{ce} = \frac{D_1}{P_0} + g = \frac{D_1}{P_0(1-g)} + g$$

float factor =  $\frac{\text{Avg daily float}}{\text{Avg daily deposit}}$

$k_{ce} = R_f + \beta[E(R_m) - R_f]$  ↳ float %

$k_{ce} = \text{bond yield} + \text{risk premium}$

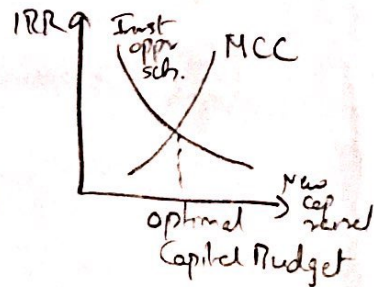
↳ This is pre-tax

unlevered asset beta:

project beta:

$$\beta_{ASSET} = \beta_{EQUITY} \left[ \frac{1}{1 + \left( (1-t) \frac{D}{E} \right)} \right]$$

$$\beta_{PROJECT} = \beta_{ASSET} \left[ 1 + \left( (1-t) \frac{D}{E} \right) \right]$$



cost of common equity with a country risk premium:

$$k_{ce} = R_f + \beta[E(R_{MKT}) - R_f + \text{country risk premium}]$$

↳ SOV-yield spread x  $\frac{\text{req. of developing}}{\text{bond of developed}}$

break point =  $\frac{\text{amount of capital at which the component's cost of capital changes}}{\text{weight of the component in the capital structure}}$

degree of operating leverage =  $\frac{QP - V}{QP - V - F} = \frac{\% \Delta EBIT}{\% \Delta \text{sales}}$

F = Fixed operating cost  
 C = " " Financing cost

degree of financial leverage =  $\frac{EBIT}{EBIT - I} = \frac{\% \Delta EPS}{\% \Delta EBIT}$

$\frac{Q(P-V) - F}{Q(P-V) - F - C} \rightarrow \text{Operating inc}$   
 $\rightarrow \text{Opt Inc - Int}$

degree of total leverage =  $DOL \times DFL = \frac{\% \Delta EPS}{\% \Delta \text{sales}}$

\* contribution margin =  $P - V$

breakeven quantity of sales =  $\frac{\text{fixed operating costs} + \text{fixed financing costs}}{\text{price} - \text{variable cost per unit}}$

operating breakeven quantity of sales =  $\frac{\text{fixed operating costs}}{\text{price} - \text{variable cost per unit}}$

$$\text{current ratio} = \frac{\text{current assets}}{\text{current liabilities}}$$

$$\text{quick ratio} = \frac{\text{cash} + \text{short-term marketable securities} + \text{receivables}}{\text{current liabilities}}$$

$$\text{receivables turnover} = \frac{\text{credit sales}}{\text{average receivables}}$$

$$\text{number of days of receivables} = \frac{365}{\text{receivables turnover}} = \frac{\text{average receivables}}{\text{average day's credit sales}}$$

$$\text{inventory turnover} = \frac{\text{cost of goods sold}}{\text{average inventory}}$$

$$\text{number of days of inventory} = \frac{365}{\text{inventory turnover}} = \frac{\text{average inventory}}{\text{average day's COGS}}$$

$$\text{payables turnover ratio} = \frac{\text{purchases} \rightarrow \text{COGS} + \Delta \text{Inv.}}{\text{average trade payables}}$$

$$\text{number of days of payables} = \frac{365}{\text{payables turnover ratio}} = \frac{\text{average payables}}{\text{average day's purchases}}$$

$$\text{operating cycle} = \text{average days of inventory} + \text{average days of receivables}$$

$$\text{cash conversion cycle} = \left( \text{average days of receivables} \right) + \left( \text{average days of inventory} \right) - \left( \text{average days of payables} \right)$$

$$\% \text{ discount} = \left( \frac{\text{face value} - \text{price}}{\text{face value}} \right)$$

$$\text{discount-basis yield} = \left( \frac{\text{face value} - \text{price}}{\text{face value}} \right) \left( \frac{360}{\text{days}} \right) = \% \text{ discount} \times \left( \frac{360}{\text{days}} \right)$$

$$\text{money market yield} = \left( \frac{\text{face value} - \text{price}}{\text{price}} \right) \left( \frac{360}{\text{days}} \right)$$

$$= \text{holding period yield} \times \left( \frac{360}{\text{days}} \right)$$

Add-on yield

$$\text{bond equivalent yield} = \left( \frac{\text{face value} - \text{price}}{\text{price}} \right) \left( \frac{365}{\text{days to maturity}} \right)$$

$$= \text{holding period yield} \times \left( \frac{365}{\text{days}} \right)$$

Cost of not taking the disc

$$\text{cost of trade credit} = \left( 1 + \frac{\% \text{ discount}}{1 - \% \text{ discount}} \right)^{\frac{365}{\text{days past discount}}} - 1$$

where:

$$\text{days past discount} = \text{number of days after the end of the discount period}$$

$$\text{holding period return} = \frac{\text{end-of-period value}}{\text{beginning-of-period value}} - 1$$

$$= \frac{P_t + \text{Div}_t}{P_0} - 1 = \frac{P_t - P_0 + \text{Div}_t}{P_0}$$

If cost trade credit > returns from fund → avail discount

→ If 2/10 net 40  
then 40 - 10 = 30 is days past disc

$$\text{mean return} = \frac{(R_1 + R_2 + R_3 + \dots + R_n)}{n}$$

$$\text{geometric mean return} = \sqrt[n]{(1 + R_1) \times (1 + R_2) \times (1 + R_3) \times \dots \times (1 + R_n)} - 1$$

$$\text{population variance from historical data: } \sigma^2 = \frac{\sum_{t=1}^T (R_t - \mu)^2}{T}$$

$$\text{sample variance from historical data: } s^2 = \frac{\sum_{t=1}^T (R_t - \bar{R})^2}{T - 1}$$

$$\text{sample covariance from historical data: } \text{Cov}_{1,2} = \frac{\sum_{t=1}^n \{ [R_{t,1} - \bar{R}_1] [R_{t,2} - \bar{R}_2] \}}{n - 1}$$

$$\text{correlation: } \rho_{1,2} = \frac{\text{Cov}_{1,2}}{\sigma_1 \times \sigma_2}$$

standard deviation for a two-asset portfolio:

$$\sigma_p = \sqrt{w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2 w_1 w_2 \sigma_1 \sigma_2 \rho_{1,2}} \text{ or } \sqrt{w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2 w_1 w_2 \text{Cov}_{1,2}}$$

$$\text{equation of the CML: } E(R_p) = R_f + \left( \frac{E(R_M) - R_f}{\sigma_M} \right) \sigma_p$$

$$E(R_p) = R_f + (E(R_M) - R_f) \left( \frac{\sigma_p}{\sigma_M} \right)$$

total risk = systematic risk + unsystematic risk

$$\beta_i = \frac{\text{Cov}_{i,\text{mkt}}}{\sigma_{\text{mkt}}^2} = \rho_{i,\text{mkt}} \frac{\sigma_i}{\sigma_{\text{mkt}}}$$

$$\text{capital asset pricing model (CAPM): } E(R_i) = R_f + \beta_i [E(R_{\text{mkt}}) - R_f]$$

$$\text{margin call price} = P_0 \left( \frac{1 - \text{initial margin}}{1 - \text{maintenance margin}} \right)$$

aKa initial equity =  $\frac{1}{\text{leverage ratio}}$

$$\text{price-weighted index} = \frac{\text{sum of stock prices}}{\text{number of stocks in index adjusted for splits}}$$

$$\text{market cap-weighted index} = \frac{\sum [(price_{\text{today}}) (\text{number of shares outstanding})]}{\sum [(price_{\text{base year}}) (\text{number of shares outstanding})]}$$

× base year index value



preferred stock valuation model:  $P_0 = \frac{D_p}{k_p}$

one-period stock valuation model:  $P_0 = \frac{D_1}{1+k_e} + \frac{P_1}{1+k_e}$

infinite period model:  $P_0 = \frac{D_1}{k_e - g} = \frac{D_0 \times (1+g)}{k_e - g}$

multistage model:

$$P_0 = \frac{D_1}{(1+k_e)} + \frac{D_2}{(1+k_e)^2} + \dots + \frac{D_n}{(1+k_e)^n} + \frac{P_n}{(1+k_e)^n}$$

where:

$P_n = \frac{D_{n+1}}{k_e - g_c}$ , and  $D_{n+1}$  is a dividend that will grow at the constant rate of  $g_c$  forever

earnings multiplier:  $\frac{P_0}{E_1} = \frac{\left(\frac{D_1}{E_1}\right)}{k-g}$   $\rightarrow$  Divid. payout ratio

expected growth rate:  $g = (\text{retention rate})(\text{ROE})$   $\rightarrow 1 - \text{dividend payout ratio}$

trailing P/E =  $\frac{\text{market price per share}}{\text{EPS over previous 12 months}}$

leading P/E =  $\frac{\text{market price per share}}{\text{forecast EPS over next 12 months}}$

P/B ratio =  $\frac{\text{market value of equity}}{\text{book value of equity}} = \frac{\text{market price per share}}{\text{book value per share}}$

where:

book value of equity = common shareholders' equity  
= (total assets - total liabilities) - preferred stock

P/S ratio =  $\frac{\text{market value of equity}}{\text{total sales}} = \frac{\text{market price per share}}{\text{sales per share}}$

P/CF ratio =  $\frac{\text{market value of equity}}{\text{cash flow}} = \frac{\text{market price per share}}{\text{cash flow per share}}$

enterprise value = market value of common and preferred stock  
+ market value of debt  
- cash and short-term investments

$$\frac{\text{net inc} - \text{pry. dividends}}{\text{wt. avg. no. of common shares outstanding}}$$

EPS = 
$$\frac{\text{net inc}}{\text{wt. avg. no. of common shares} + \text{New shares if convt. shares are converted.}}$$

• Cash paid for new equip = Ending gross equip. bal + Gross cost of equip sold - Beg. gross ep. bal

↑  
Beg. Bal - End Bal + Equip purch. (BB)

• Cash from Sale = Historical cost of equip. sold - Depr. on Equip. sold + Gain on Sale of ep.

↑  
BB Ep. + EB Equip + Ep purch

↑  
BB of Acc Depr. - EB of Acc Depr. + Depr. Exp.

• Net CF from Creditors = New borrowings - Principle amt repaid

• Net CF from Shareholders = New Equity issued - Shares repurch. - Cash div paid

• FCFF = CFO + Int (1 - Tax Rate) - Fixed Cap. Inv

↓  
Net inc + Non cash charges - Working Cap

• FCFE = CFO + Net borrowing - Fixed Cap Inv

= CFO - Net debt repmt - Fixed cap inv.

$$OCI = CI - NI$$

ratios:

$$\text{receivables turnover} = \frac{\text{annual sales}}{\text{average receivables}}$$

$$\text{days of sales outstanding} = \frac{365}{\text{receivables turnover}}$$

$$\text{inventory turnover} = \frac{\text{cost of goods sold}}{\text{average inventory}}$$

$$\text{days of inventory on hand} = \frac{365}{\text{inventory turnover}}$$

$$\text{payables turnover} = \frac{\text{purchases}}{\text{average trade payables}} \rightarrow \text{COGS} + \Delta \text{Inv}$$

$$\text{number of days of payables} = \frac{365}{\text{payables turnover ratio}}$$

$$\text{total asset turnover} = \frac{\text{revenue}}{\text{average total assets}}$$

$$\text{fixed asset turnover} = \frac{\text{revenue}}{\text{average net fixed assets}}$$

$$\text{working capital turnover} = \frac{\text{revenue}}{\text{average working capital}}$$

**Liquidity Ratios:**

$$\text{current ratio} = \frac{\text{current assets}}{\text{current liabilities}}$$

$$\text{quick ratio} = \frac{\text{cash} + \text{marketable securities} + \text{receivables}}{\text{current liabilities}}$$

$$\text{cash ratio} = \frac{\text{cash} + \text{marketable securities}}{\text{current liabilities}}$$

$$\text{defensive interval} = \frac{\text{cash} + \text{marketable securities} + \text{receivables}}{\text{average daily expenditures}}$$

$$\text{cash conversion cycle} = \left( \frac{\text{days sales}}{\text{outstanding}} \right) + \left( \frac{\text{days of inventory}}{\text{on hand}} \right) - \left( \frac{\text{number of days}}{\text{of payables}} \right)$$

**Solvency Ratios:**

$$\text{debt-to-equity} = \frac{\text{total debt}}{\text{total shareholders' equity}}$$

$$\text{debt-to-capital} = \frac{\text{total debt}}{\text{total debt} + \text{total shareholders' equity}}$$

Bonds payable = PV of bond + disc - prem.

$$\text{debt-to-assets} = \frac{\text{total debt}}{\text{total assets}}$$

$$\text{financial leverage} = \frac{\text{average total assets}}{\text{average total equity}}$$

$$\text{interest coverage} = \frac{\text{earnings before interest and taxes}}{\text{interest payments}}$$

Net inc + (nt exp) + tax paid  
observe the diff

$$\text{fixed charge coverage} = \frac{\text{earnings before interest and taxes} + \text{lease payments}}{\text{interest payments} + \text{lease payments}}$$

### Profitability Ratios:

$$\text{net profit margin} = \frac{\text{net income}}{\text{revenue}}$$

$$\text{gross profit margin} = \frac{\text{gross profit}}{\text{revenue}}$$

$$\text{operating profit margin} = \frac{\text{operating income}}{\text{revenue}} \text{ or } \frac{\text{EBIT}}{\text{revenue}}$$

$$\text{pretax margin} = \frac{\text{EBT}}{\text{revenue}}$$

$$\text{return on assets (ROA)} = \frac{\text{net income}}{\text{average total assets}}$$

$$\text{return on assets (ROA)} = \frac{\text{net income} + \text{interest expense} (1 - \text{tax rate})}{\text{average total assets}}$$

$$\text{operating return on assets} = \frac{\text{operating income}}{\text{average total assets}} \text{ or } \frac{\text{EBIT}}{\text{average total assets}}$$

$$\star \text{ return on total capital} = \frac{\text{EBIT}}{\text{average total capital}}$$

$$\text{return on equity} = \frac{\text{net income}}{\text{average total equity}}$$

$$\text{return on common equity} = \frac{\text{net income} - \text{preferred dividends}}{\text{average common equity}}$$

$$= \frac{\text{net income available to common}}{\text{average common equity}}$$

### Free Cash Flow to the Firm:

$$\text{FCFF} = \text{net income} + \text{noncash charges} + [\text{cash interest paid} \times (1 - \text{tax rate})] - \text{fixed capital investment} - \text{working capital investment}$$

$$\text{FCFF} = \text{cash flow from operations} + [\text{cash interest paid} \times (1 - \text{tax rate})] - \text{fixed capital investment}$$

### Cash Flow to Equity:

FCFE = cash flow from operations – fixed capital investment + net borrowing

common-size income statement ratios =  $\frac{\text{income statement account}}{\text{sales}}$

common-size balance sheet ratios =  $\frac{\text{balance sheet account}}{\text{total assets}}$

common-size cash flow ratios =  $\frac{\text{cash flow statement account}}{\text{revenues}}$

original DuPont equation:  $\text{ROE} = \left(\frac{\text{net profit}}{\text{margin}}\right) \left(\frac{\text{asset}}{\text{turnover}}\right) \left(\frac{\text{leverage}}{\text{ratio}}\right)$

extended DuPont equation: = ROA x fin leverage

$\text{ROE} = \left(\frac{\text{net income}}{\text{EBT}}\right) \left(\frac{\text{EBT}}{\text{EBIT}}\right) \left(\frac{\text{EBIT}}{\text{revenue}}\right) \left(\frac{\text{revenue}}{\text{total assets}}\right) \left(\frac{\text{total assets}}{\text{total equity}}\right)$

basic EPS =  $\frac{\text{net income} - \text{preferred dividends}}{\text{weighted average number of common shares outstanding}}$

diluted EPS =

$$\frac{\left[\text{net income} - \text{preferred dividends}\right] + \left[\frac{\text{convertible preferred}}{\text{dividends}}\right] + \left(\frac{\text{convertible debt}}{\text{interest}}\right)(1-t)}{\left(\frac{\text{weighted average}}{\text{shares}}\right) + \left(\frac{\text{shares from conversion of conv. pfd. shares}}{\text{conv. pfd. shares}}\right) + \left(\frac{\text{shares from conversion of conv. debt}}{\text{conv. debt}}\right) + \left(\frac{\text{shares issuable from stock options}}{\text{stock options}}\right)}$$

### Coefficients of Variation:

$\text{CV sales} = \frac{\text{standard deviation of sales}}{\text{mean sales}}$

$\text{CV operating income} = \frac{\text{standard deviation of operating income}}{\text{mean operating income}}$

$\text{CV net income} = \frac{\text{standard deviation of net income}}{\text{mean net income}}$

### Inventories:

ending inventory = beginning inventory + purchases – COGS

FIFO COGS = LIFO COGS – (ending LIFO reserve – beginning LIFO reserve)

FIFO inv = LIFO inv + LIFO reserve (1-T)

FIFO NI = LIFO NI + ΔLIFO reserve (1-T)

FIFO Ret Earnings = LIFO RE + LIFO res. (1-T)

**Long-Lived Assets:**

$$\text{straight-line depreciation} = \frac{\text{cost} - \text{salvage value}}{\text{useful life}}$$

$$\text{DDB depreciation} = \left( \frac{2}{\text{useful life}} \right) (\text{cost} - \text{accumulated depreciation})$$

$$\text{units-of-production depreciation} = \frac{\text{original cost} - \text{salvage value}}{\text{life in output units}} \times \text{output units in the period}$$

$$\text{average age} = \frac{\text{accumulated depreciation}}{\text{annual depreciation expense}}$$

$$\text{total useful life} = \frac{\text{historical cost}}{\text{annual depreciation expense}}$$

$$\text{remaining useful life} = \frac{\text{ending net PP\&E}}{\text{annual depreciation expense}}$$

DTL if  $ITE > ITP$   
else DTA

Def. Tax Liab

$$= (\text{Carrying amt} - \text{Tax Base}) \times \text{Tax Rate}$$

Reported Tax Rate

$$= \frac{\text{Int. exp}}{\text{Pretax inc}}$$

unded Assets

$$= \text{Plan Assets} -$$

$$\text{PV (est. pension obligation)}$$

**Deferred Taxes:**

$$\text{income tax expense} = \text{taxes payable} + \Delta \text{DTL} - \Delta \text{DTA}$$

**Debt Liabilities:**

$$\text{interest paid} = \text{Cpn rate} \times \text{Issued amt}_{i,t} (\text{Final Val.})$$

$$\text{interest expense} = \left( \frac{\text{the market rate at issue (YTM)}}{\text{the balance sheet value of the liability at the beginning of the period}} \right)$$

$$\text{Amortizat of disc} = \text{int. exp} - \text{int. paid}$$

**Performance Ratios:**

$$\text{cash flow-to-revenue} = \frac{\text{CFO}}{\text{net revenue}}$$

$$\text{cash return-on-assets} = \frac{\text{CFO}}{\text{average total assets}}$$

$$\text{cash return-on-equity} = \frac{\text{CFO}}{\text{average total equity}}$$

$$\text{cash-to-income} = \frac{\text{CFO}}{\text{operating income}}$$

$$\text{cash flow per share} = \frac{\text{CFO} - \text{preferred dividends}}{\text{weighted average number of common shares}}$$

**Key Ratios:**

$$\text{debt coverage} = \frac{\text{CFO}}{\text{total debt}}$$

$$\text{interest coverage} = \frac{\text{CFO} + \text{interest paid} + \text{taxes paid}}{\text{interest paid}}$$

$$\text{reinvestment} = \frac{\text{CFO}}{\text{cash paid for long-term assets}}$$

$$\text{debt payment} = \frac{\text{CFO}}{\text{cash long-term debt repayment}}$$

$$\text{dividend payment} = \frac{\text{CFO}}{\text{dividends paid}}$$

$$\text{investing and financing} = \frac{\text{CFO}}{\text{cash outflows from investing and financing activities}}$$

# MULAS

nominal risk-free rate = real risk-free rate + expected inflation rate

required interest rate on a security = nominal risk-free rate  
 + default risk premium  
 + liquidity premium  
 + maturity risk premium

effective annual rate =  $(1 + \text{periodic rate})^m - 1$

continuous compounding:  $e^r - 1 = \text{EAR}$

$PV_{\text{perpetuity}} = \frac{PMT}{I/Y}$

• PV of annuity due = PV of ordinary annuity \*  $(1 + I/Y)$

$FV = PV(1 + I/Y)^N$

• FV of ann. due = PV of ord. ann. \*  $(1 + I/Y)$

$NPV = \sum_{t=0}^N \frac{CF_t}{(1+r)^t}$  → discounted at opportunity cost of capital

general formula for the IRR:  $0 = CF_0 + \frac{CF_1}{1+IRR} + \frac{CF_2}{(1+IRR)^2} + \dots + \frac{CF_N}{(1+IRR)^N}$

• If  $IRR > \text{disc rate}$ : NPV +ve  
 • If  $IRR < \text{disc rate}$ : NPV -ve

bank discount yield =  $\frac{D}{F} \times \frac{360}{t}$

• NPV & IRR give same results when projects are independent

holding period yield =  $\frac{P_1 - P_0 + D_1}{P_0} = \frac{P_1 + D_1}{P_0} - 1$

• Time wt. return (TWR) is preferred

• Generally,  $TWR > MWR$ .  
 • In TWR, do ~~not~~ geometric mean

only 1 return for yrs are given not for quarters  
 • If  $EAR = 9\%$ ,  
 Bond eq. yield =  $2 \left[ \left( \frac{1.09}{4} \right)^{1/2} - 1 \right] = 8.803\%$

effective annual yield =  $(1 + HPY)^{365/t} - 1$  → Compounding

money market yield =  $HPY \left( \frac{360}{t} \right) = \frac{360 \times r_{BD}}{360 - (t \times r_{BD})} = 2 \times \text{semi-annual disc rate}$

population mean:  $\mu = \frac{\sum_{i=1}^N X_i}{N}$

sample mean:  $\bar{X} = \frac{\sum_{i=1}^n X_i}{n}$

geometric mean return ( $R_G$ ):  $1 + R_G = \sqrt[n]{(1+R_1) \times (1+R_2) \times \dots \times (1+R_n)}$

geometric mean  $\leq$  Arithmetic mean.

Harmonic mean  $<$  Geometric Mean  $<$  Arithmetic Mean.  
 ↑ dollar cost avg      ↑ w/ compounding      ↑ w/o compounding  
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Measures of location = Quantile + Measures of central tendency

\* harmonic mean:  $\bar{X}_H = \frac{N}{\sum_{i=1}^N \frac{1}{x_i}}$

\* weighted mean:  $\bar{X}_w = \sum_{i=1}^n w_i X_i$

\* position of the observation at a given percentile, y:  $L_y = (n+1) \frac{y}{100}$

range = maximum value - minimum value

\* excess kurtosis = sample kurtosis - 3

\* MAD =  $\frac{\sum_{i=1}^n |X_i - \bar{X}|}{n}$

$\sigma > MAD$

Works for any distribution  
\* Chebyshev's Ineq.  
% of data that lie within K sd  
 $\boxed{1 - \frac{1}{K^2}}$  atleast

\* population variance =  $\sigma^2 = \frac{\sum_{i=1}^N (X_i - \mu)^2}{N}$

where  $\mu$  = population mean and N = number of possible outcomes

\* sample variance =  $s^2 = \frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}$ , where  $\bar{X}$  = sample mean and n = sample size

used to compare 2 dist<sup>n</sup> w/ diff means  
\* coefficient of variation:  $CV = \frac{s_x}{\bar{X}} = \frac{\text{standard deviation of } x}{\text{average value of } x}$

(Lower the better)

\* Sample skewness

$\frac{1}{n} \frac{\sum (X_i - \bar{X})^3}{s^3}$

Sharpe ratio =  $\frac{\bar{r}_p - r_f}{\sigma_p}$

\* Sample kurtosis

$\frac{1}{n} \frac{\sum (X_i - \bar{X})^4}{s^4}$

\* joint probability:  $P(AB) = P(A | B) \times P(B)$

\* addition rule:  $P(A \text{ or } B) = P(A) + P(B) - P(AB)$

\* multiplication rule:  $P(A \text{ and } B) = P(A) \times P(B)$

\* total probability rule:

$P(R) = P(R | S_1) \times P(S_1) + P(R | S_2) \times P(S_2) + \dots + P(R | S_N) \times P(S_N)$

\* expected value:  $E(X) = \sum P(x_i) x_i = P(x_1) x_1 + P(x_2) x_2 + \dots + P(x_n) x_n$

\* Cov(R<sub>i</sub>, R<sub>j</sub>) =  $E\{[R_i - E(R_i)][R_j - E(R_j)]\}$  → Range - ∞ to ∞

\* Variance =  $\sum (x_i - \bar{x})^2 \cdot P(x_i)$

\* Stating odds

If P(A) out of B trials is odd  $\frac{P(A)}{P(B) - P(A)}$  i.e.  $\frac{A}{1-A}$

Lepto > 3  
Meso = 3  
Platy < 3

$\rho(R_i, R_j) = \frac{\text{Cov}(R_i, R_j)}{\sigma(R_i)\sigma(R_j)} \rightarrow$  Strength of linear relationship.

\* portfolio expected return:  $E(R_p) = \sum_{i=1}^N w_i E(R_i) = w_1 E(R_1) + w_2 E(R_2) + \dots + w_n E(R_n)$

\* portfolio variance:  $\text{Var}(R_p) = \sum_{i=1}^N \sum_{j=1}^N w_i w_j \text{Cov}(R_i, R_j) = w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2w_1 w_2 \sigma_1 \sigma_2 \text{Cov}(1, 2)$   
 $= w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2 + 2w_1 w_2 \text{Cov}(1, 2)$

where  $w_i = \frac{\text{market value of investment in asset } i}{\text{market value of the portfolio}}$

\* Bayes' formula:

updated probability =  $\frac{\text{probability of new information for a given event}}{\text{unconditional probability of new information}} \times \text{prior probability of event}$   
 $P(B|A) = \frac{P(A|B) \cdot P(B)}{P(A)}$

\* combination (binomial) formula:  ${}_n C_r = \frac{n!}{(n-r)!r!}$

\* permutation formula:  ${}_n P_r = \frac{n!}{(n-r)!}$ . Given  $n$  items, there are  $n!$  ways to arrange them.

\* binomial probability:  $P(x) = \frac{n!}{(n-x)!x!} p^x (1-p)^{n-x}$

(probability of 'x' successes in 'n' trials)

\* for a binomial random variable:  $E(X) = np$ ; variance =  $np(1-p)$

\* for a normal variable:

90% confidence interval for  $X$  is  $\bar{X} - 1.65s$  to  $\bar{X} + 1.65s$

95% confidence interval for  $X$  is  $\bar{X} - 1.96s$  to  $\bar{X} + 1.96s$

99% confidence interval for  $X$  is  $\bar{X} - 2.58s$  to  $\bar{X} + 2.58s$

\*  $z = \frac{\text{observation} - \text{population mean}}{\text{standard deviation}} = \frac{x - \mu}{\sigma}$

Maximize  $\rightarrow$   $\frac{E(R_p) - R_L}{\sigma_p}$  means minimize  $P(R_{\text{portfolio}} < R_{\text{threshold}})$   
 no. of std. deviat below the mean.

\* continuously compounded rate of return:  $r_{cc} = \ln\left(\frac{S_1}{S_0}\right) = \ln(1 + \text{HPR})$       $\text{HPR} > R_{cc}$

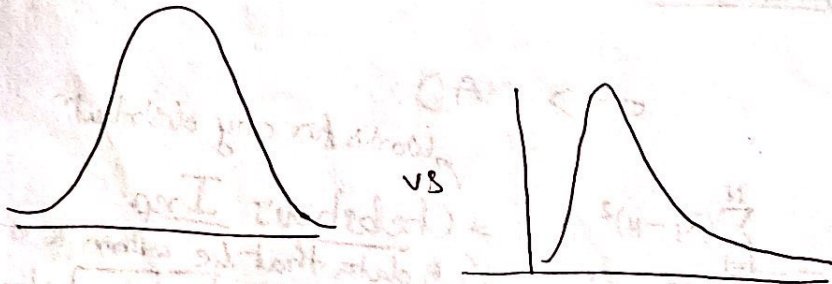
\* for a uniform distribution:  $P(x_1 \leq X \leq x_2) = \frac{(x_2 - x_1)}{(b - a)}$

If there are  $K$  steps to complete a task & each task can be done in  $n$  ways, then no. of ways to complete the task is  $n_1 \times n_2 \times n_3 \times n_4 \dots n_K$

Binomial prob. example

Consider a big bowl w/ black & white beans. Compute probab. of drawing 3 black beans. Prob. of drawing black bean is 0.6. You have chosen 5 beans.

Normal vs lognormal prob.



For multi-normal  $\rightarrow$  two distn must be dependent

$\prod (R_i, R_j) = \dots$   
 \* portfolio expected r

# Hypothesis Testing

State the hypothesis

Compute test statistic  $\rightarrow \frac{\text{Sample statistic} - \text{hypothesized val}}{\text{std error of sample stat}}$

Determine critical val. based on sig. level

Compare test stat w/ critical val. to determine whether or not to reject null hypothesis

Tests for single mean

t-stat / z-stat

Test for diff. b/w means

2 independent  $Z$  normal dist<sup>n</sup> pop<sup>n</sup>

Test for mean of diff. (Paired comp) dependent pop<sup>n</sup>

Test for single var.

Chi-squared test

If dof = 23 & 5% sig. level then look @ dof 23 & 0.025 and dof 23 & 0.975 for critical values

Type I error  $\rightarrow$  Rejecting null hypo even when its true  
 II  $\rightarrow$  Accepting false

$\alpha = P(\text{Type I error})$

P-value  $\propto \frac{1}{t\text{-stat}}$

t-test / z-test  $\rightarrow$  Mean of 1 normal dist<sup>n</sup>

Diff in mean  $\rightarrow$  2

Mean diff  $\rightarrow$  2

$\chi^2$ -test  $\rightarrow$  Variance of 1

F-test  $\rightarrow$  Variance of 2

2 independent } critical val. using  
 2 independent } t-dist

Short-int. ratio =  $\frac{\text{No. of shares inv. sold short}}{\text{Avg. daily vol.}}$

Momentum / Rate of Change Osc (M) =  $(V - V_x) \times 100$  { V = last closing price }

Relative Strength Index =  $100 - \frac{100}{1+RS}$   $\rightarrow \frac{\text{Total price } \uparrow}{\text{Total price } \downarrow}$

% K line =  $\frac{\text{Latest price} - \text{low}}{\text{High} - \text{low}}$

Elliot Wave theory : Fib ratios converge to 0.618 or 1.618

Amis index	No. of adv. issues	No. of decl. issues
	Vol. of adv. issues	Vol. of decl. issues
$\approx 1$	balanced	
$< 1$	$\uparrow$ money in adv. stocks $\rightarrow$ buying mood	
$> 1$	decl. $\rightarrow$ selling	

unpaired test

sampling error of the mean = sample mean - population mean =  $\bar{x} - \mu$

standard error of the sample mean, known population variance:  $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$

standard error of the sample mean, unknown population variance:  $s_{\bar{x}} = \frac{s}{\sqrt{n}}$

confidence interval: point estimate  $\pm$  (reliability factor  $\times$  standard error)

$\alpha$  = level of significance  
 $1 - \alpha$  = degree of confid.

confidence interval for the population mean:  $\bar{x} \pm z_{\alpha/2} \left( \frac{\sigma}{\sqrt{n}} \right)$  for sample

t-distrib

tests for population mean =  $\mu_0$ : z-statistic =  $\frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$ , t-statistic =  $\frac{\bar{x} - \mu_0}{s / \sqrt{n}}$

for one-tailed, use  $\alpha$   
two-tailed, use  $\frac{\alpha}{2}$

test for equality of variances:  $F = \frac{s_1^2}{s_2^2}$ , where  $s_1^2 > s_2^2$

So if  $n = 30$  & 90% confid interval,

paired comparisons test: t-statistic =  $\frac{\bar{d} - \mu_{dz}}{s_{\bar{d}}}$

Power of test =  $1 - P(\text{Type 2 err})$

p-val < sig. level  $\rightarrow$  Reject  $H_0$

for one-tailed, 29 df  $\alpha = 0.10$   
two, 29 df  $\alpha = 0.05$

test for differences in means:

t-statistic =  $\frac{(\bar{x}_1 - \bar{x}_2)}{\left( \frac{s_1^2}{n_1} + \frac{s_2^2}{n_2} \right)^{1/2}}$  (sample variances assumed unequal)

Chi-square =  $\frac{(n-1) \text{ sample var}}{\text{hypo var}}$

If you are calculating  $\bar{x} \pm$  critical val  $\times$  std dev<sup>n</sup>

t-statistic =  $\frac{(\bar{x}_1 - \bar{x}_2)}{\left( \frac{s_p^2}{n_1} + \frac{s_p^2}{n_2} \right)^{1/2}}$  (sample variances assumed equal)

for a sample,

then use  $\bar{x} \pm$  critical val  $\times \frac{\sigma}{\sqrt{n}}$

pop<sup>n</sup> var known  $\rightarrow$  z dist<sup>n</sup>  
unknown  $\rightarrow$  t dist<sup>n</sup>

Relative Strength Analysis =  $\frac{\text{Price of SHK}}{\text{Price of benchmark}}$   
Head & Shoulders = Neckline - (Head - Neckline)  
Inv. Head & Shld. = Neckline + (Neckline - Head)

Central limit theorem: Sampling dist<sup>n</sup>'s  $\mu' = \text{Pop}^n \mu$   
 $\sigma^2 = \frac{\sigma^2}{n}$

Time Series Data: Obs taken over time & equally spaced interval

Cross Sectional: Sample of obs taken at a single pt in time

Longitudinal: Obs taken over time & multiple characteristics of same comp.

Panel data: Obs over time of same characteristic of diff. entities

# MULAS

for an annual-coupon bond with  $N$  years to maturity:

$$\text{price} = \frac{\text{coupon}}{(1 + \text{YTM})} + \frac{\text{coupon}}{(1 + \text{YTM})^2} + \dots + \frac{\text{coupon} + \text{principal}}{(1 + \text{YTM})^N}$$

•  $PV_{\text{full}} = PV_{\text{flat}} + AI$   
 •  $PV_{\text{full}} = PV \text{ of the bond} \times (1 + \text{YTM})^{t/T}$

for a semiannual-coupon bond with  $N$  years to maturity:

$$\text{price} = \frac{\text{coupon}}{\left(1 + \frac{\text{YTM}}{2}\right)} + \frac{\text{coupon}}{\left(1 + \frac{\text{YTM}}{2}\right)^2} + \dots + \frac{\text{coupon} + \text{principal}}{\left(1 + \frac{\text{YTM}}{2}\right)^{N \times 2}}$$

•  $AI = \frac{\text{time since last cpn pmt till settle date}}{T (\text{ie } 360)} \times \text{cpn pmt}$

bond value using spot rates:

$$\text{no-arbitrage price} = \frac{\text{coupon}}{(1 + S_1)} + \frac{\text{coupon}}{(1 + S_2)^2} + \dots + \frac{\text{coupon} + \text{principal}}{(1 + S_N)^N}$$

full price between coupon payment dates:

(Bond value at last coupon date based on the current YTM)  $\times (1 + \text{YTM}/\#)^{t/T}$   
 where # is the number of coupon periods per year,  $t$  is the number of days from the last coupon payment date until the date the bond trade will settle, and  $T$  is the number of days in the coupon period.

•  $\text{Coupon rate} = \text{Cpn rate} - L \times \text{LIBOR}$   
 if  $L < 1 \rightarrow$  unleveraged

flat price = full price - accrued interest

current yield =  $\frac{\text{annual cash coupon payment}}{\text{bond price}}$

• simple yield =  $\frac{\text{sum of annual cpn pmt} + \text{st-lone disc (cpn?)}}{\text{flat price}}$

forward and spot rates:  $(1 + S_2)^2 = (1 + S_1)(1 + 1y1y)$

option-adjusted spread:  $\text{OAS} = \text{Z-spread} - \text{option value}$

• Single month mortality =  $\frac{\text{Prepmt. for a month}}{\text{Beg. mont. bal. for month} - \text{Sched. princ. repmt for month}}$   
 • MacDwr =  $\text{Prnt wt avg of PV of all cash flows}$

modified duration =  $\frac{\text{Macaulay duration}}{1 + \text{YTM}}$   
 approx % change in bond price =  $-\text{ModDwr} \times \Delta \text{YTM}$   
approximate modified duration =  $\frac{V_- - V_+}{2V_0 \Delta \text{YTM}}$

• MacDwr for non-callable perpetual bond =  $\frac{1 + r}{r}$   
 $r \leftarrow \text{YTM}$

money duration = annual modified duration  $\times$  full price of bond position

money duration per 100 units of par value =

annual modified duration  $\times$  full bond price per 100 of par value

price value of a basis point:  $\text{PVBP} = [(V_- - V_+) / 2]$

•  $\text{Loss severity} = 1 - \text{Recov. Rate}$   
 •  $\text{Exp. loss} = \text{Default risk} \times \text{loss severity}$

approximate convexity =  $\frac{V_- + V_+ - 2V_0}{(\Delta \text{YTM})^2 V_0}$

approximate effective convexity =  $\frac{V_- + V_+ - 2V_0}{(\Delta \text{curve})^2 V_0}$

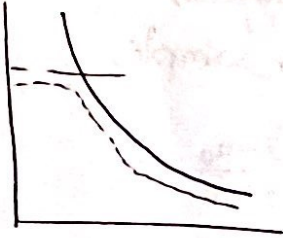
• Floating Rate Notes

Use LIBOR + Quoted Margin for cpn rate

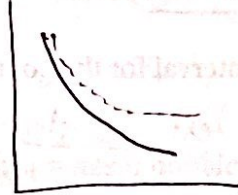
LIBOR + Rep. Margin for FRN to return to par val

• Effective Convexity

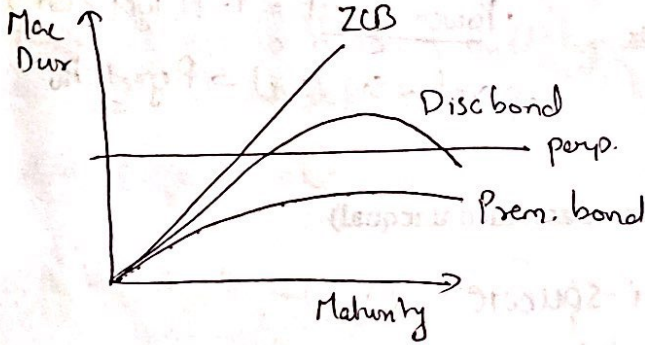
Callable bonds → -ve when  $YTM < cpn\ rate$



Puttable bonds → Always +ve

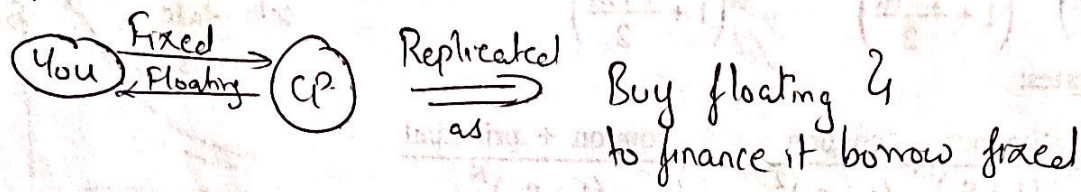


• MacDwr

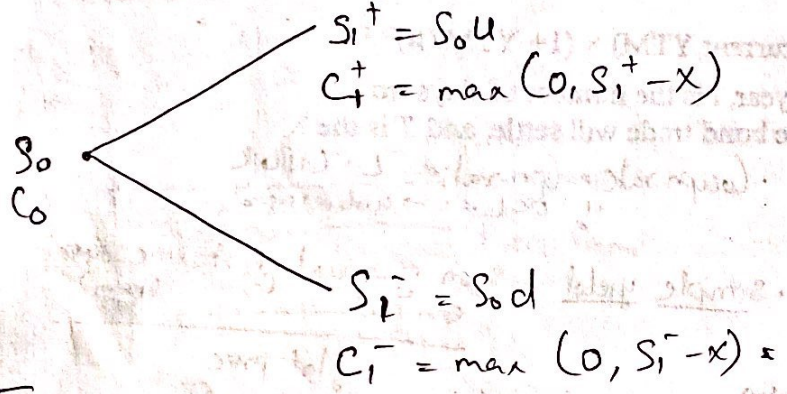


	Price	Value
Fwd	$S_T(1+r)^T$	$0 @ mt^2$
Futures	+ve correl w/ int rate	$\uparrow$ along the way
Swaps	fixed rate	PV (of cash flows)

Swaps



Binomial value of Opt<sup>n</sup>



To get expected value of call/put at  $t=1$  calc

Risk-neutral probab  $(\pi) = \frac{1 + r_f - d}{u - d}$

then calc.  $[\pi \cdot C_1^+ + (1 - \pi) \cdot C_1^-]$

then val. @  $t=0 = \frac{\downarrow}{1 + r_f}$

Volatility of underlying:  $\frac{S_1^+ - S_1^-}{S_0}$

In put-call-fwd parity, if put w/ fwd expires out of money, payoff  $\rightarrow$  mkt val. of underlying asset  
 In-the money  $\rightarrow$  FV of bond  
 for call  $\rightarrow$  reverse



$$\% \Delta \text{ full bond price} = -\text{annual modified duration}(\Delta \text{YTM}) + \frac{1}{2} \text{ annual convexity}(\Delta \text{YTM})^2$$

$$\text{duration gap} = \text{Macaulay duration} - \text{investment horizon}$$

$$\text{return impact} \approx -\text{duration} \times \Delta \text{spread} + \frac{1}{2} \text{convexity} \times (\Delta \text{spread})^2$$

$$\text{risky asset} + \text{derivative} = \text{risk-free asset}$$

$$\text{risky asset} - \text{risk-free asset} = -\text{derivative position}$$

$$\text{derivative position} - \text{risk-free asset} = -\text{risky asset}$$

$$\times \text{no-arbitrage forward price: } F_0(T) = S_0 (1 + R_f)^T$$

$$\times \text{payoff to long forward at expiration} = S_T - F_0(T)$$

$$\times \text{value of forward at time } t: V_t(T) = S_t + PV_t(\text{cost}) - PV_t(\text{benefit}) - \frac{F_0(T)}{(1 + R_f)^{T-t}}$$

$$\text{intrinsic value of a call} = \text{Max}[0, S - X]$$

$$\text{intrinsic value of a put} = \text{Max}[0, X - S]$$

$$\text{option value} = \text{intrinsic value} + \text{time value}$$

$$\text{put-call parity: } c + X / (1 + R_f)^T = S + p$$

$$\text{put-call-forward parity: } F_0(T) / (1 + R_f)^T + p_0 = c_0 + X / (1 + R_f)^T$$

$$\bullet \text{ Price of underlying} = \frac{E(S_T)}{(1+r)^T} + \frac{\gamma}{(1+r)^T} - \theta \leftarrow \text{PV of costs of holding assets}$$

$\uparrow$   
 PV of benefit  
 $\uparrow$   
 risk premium

$$\bullet \text{ Cost of carry} = \theta - \gamma$$

$$\bullet \text{ Forward Price} = \text{Spot price} (1+r)^T$$

$$\bullet \text{ Value @ initiation} = 0$$

$$\bullet \text{ Value @ end} = \text{Spot price}_T - \text{Fwd price}$$

$$\bullet \text{ Value during life of contract} = \text{Spot price}_T - \frac{\text{Fwd price}}{(1+r)^t}$$

$$\bullet \text{ Value during life of contract w/ cost \& benefits} = \text{Spot price}_T - \frac{\text{Fwd price}}{(1+r)^t} - (\gamma - \theta)(1+r)^t$$

$$\bullet \text{ Fwd price w/ cost \& benefits} = (\text{Spot price} + \theta - \gamma) (1+r)^T$$

$$\bullet \text{ Asset} - \text{Forward} = \text{Risk free} \rightarrow \text{Asset} = \text{Risk free} + \text{Fwd price}$$

$$\text{Asset} + \text{Put} = \text{Risk free} + \text{Fwd} + \text{put}$$

$$\text{Call} + \text{Bond} = \text{PV(Fwd)} + \text{put}$$

Least price ready to be paid for Call optn  
 $= C_0 \geq \text{Max}(0, S_0 - \frac{X}{(1+r)^T})$

Least price ready to be paid for Put optn  
 $= P_0 \geq \text{Max}(0, \frac{X}{(1+r)^T} - S_0)$

Fiduciary Call = Protective Put  
 Call + PV(2CBS) = STK price + Put  
 Call + PV(2CBS) = PV(Bond) + Put + Fwd

2CBS = 2x Cost of Basis

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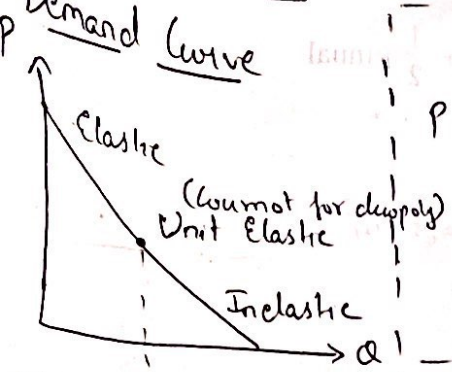
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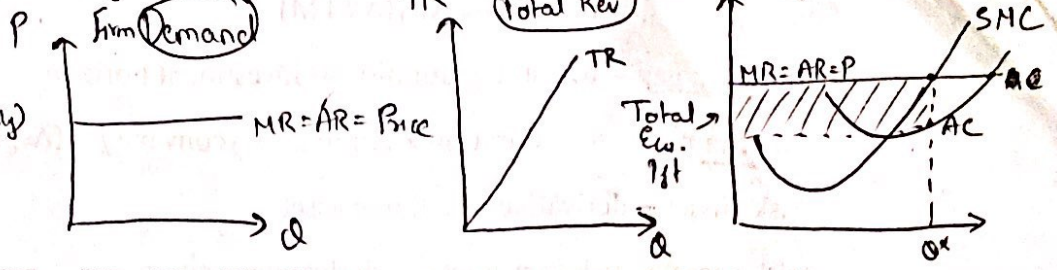
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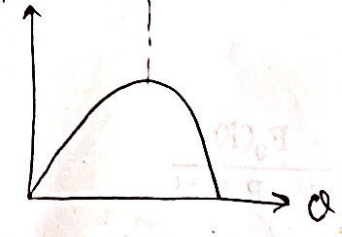
Economic Curves



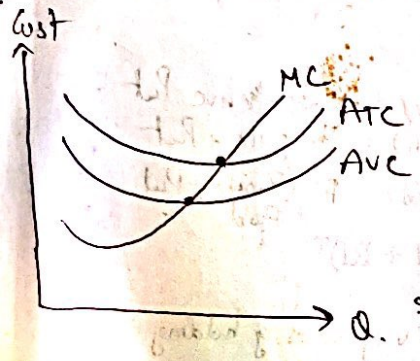
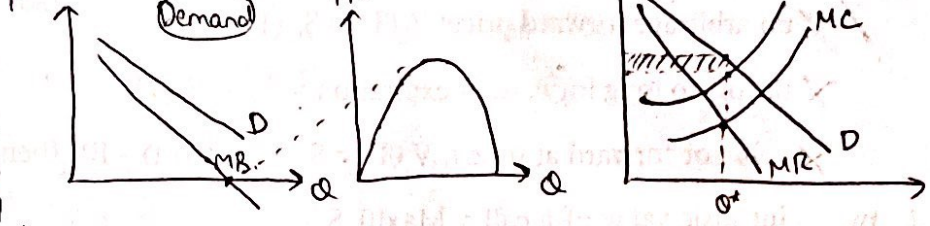
Perfect Competit<sup>n</sup>



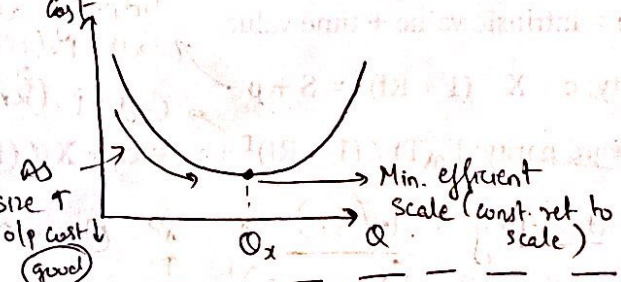
Total Expenditure



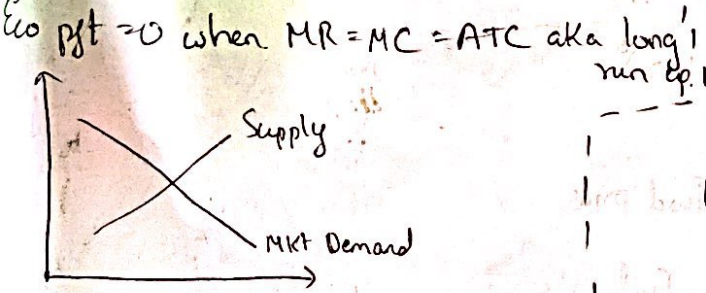
Imperfect competit<sup>n</sup>



Long-run avg. cost curve



Perfect Compet<sup>n</sup>



Supply curve related to MC as long as  $MC \geq ATC$

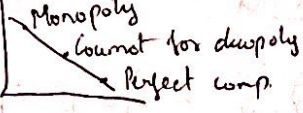
Oligopoly

MKT demands based on:  
 ↳ Pricing interdependence (Kinked DC)  
 Will follow price ↓ but will not follow price ↑



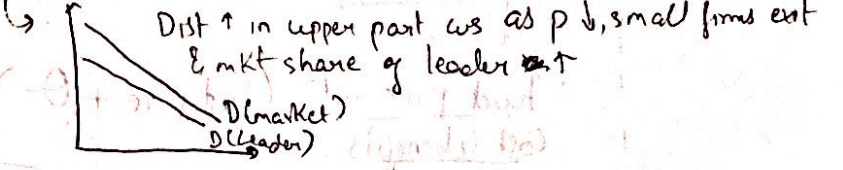
Cournot assumpt<sup>n</sup>

Each firm determines profit-max ptly assuming other firms of p will not change



Monopolistic

$P \uparrow$  &  $Q \downarrow$  than competitive  
 Supply fn not defined  
 Eco profit not poss.



↳ No optimal single price  
 ↳ Eco profit possible

Monopoly

Final price when  $MR = MC$  &  $\frac{\Delta \text{profit}}{\Delta Q} = 0$   
 MC to avoid Cournot take care of consumer surplus

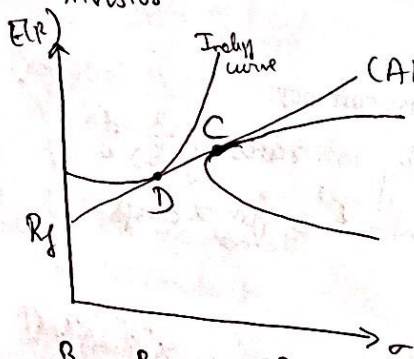
# Portfolio Mngmt

• Diversification Ratio =  $\frac{\text{Risk of equally wt. portfolio of } n \text{ securities}}{\text{Risk of single security selected @ random}}$

•  $(1 + \text{Return after tax}) = (1 + \text{Real Return})(1 + \text{inflat}^n \text{ rate})$

• Covariance =  $\sum \frac{(x_i - \bar{x})(y_i - \bar{y})}{n-1}$

• Utility of investor =  $E(r) - \frac{1}{2} A \sigma^2$



C → Best combo of risky assets (Optimal Risky port.)

D → Best combo of risky + risk free (Optimal port.)

CAL → Inv. think there are multiple eff. portfolios  
 CML → Inv. think there is only 1 risky eff. portfolio viz. mkt portfolio

•  $\beta = \beta_a w_a + \beta_b w_b$

• Total variance = Syst. var. + Non-Syst. var.  
 $(\beta_i^2 \sigma_m^2) \quad (\sigma_e^2)$

• Only  $\beta$ /Syst. Risk is priced & earns a return.

## CML

## SML

## Sec. Characteristic Line (SCL)

Slope = Sharpe  
 Applies to eff. port  
 Uses total risk

Repr. of CAPM  
 Slope = Risk premium  
 App. to any security  
 Uses syst. risk

Plots  $R_i - R_f$  vs  $R_m - R_f$

Normal ret = Real ret × Inflat Risk free  
 Real ret = Risk pre × Risk free

• Sharpe Ratio =  $\frac{R_p - R_f}{\sigma_p}$

• M2 =  $\frac{(R_p - R_f)}{\sigma_p} \cdot \sigma_m - (R_m - R_f)$  → Total risk

• Treynor =  $\frac{R_p - R_f}{\beta_p}$  → = 0 Mngr doesn't add val > 1 good

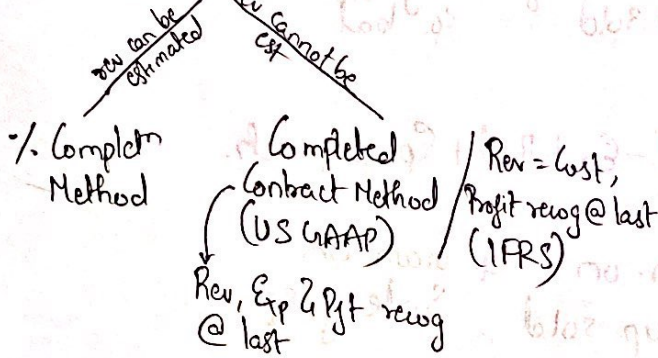
• Jensen's alpha =  $R_p - [R_f + \beta(R_m - R_f)]$  → Best one

FRA

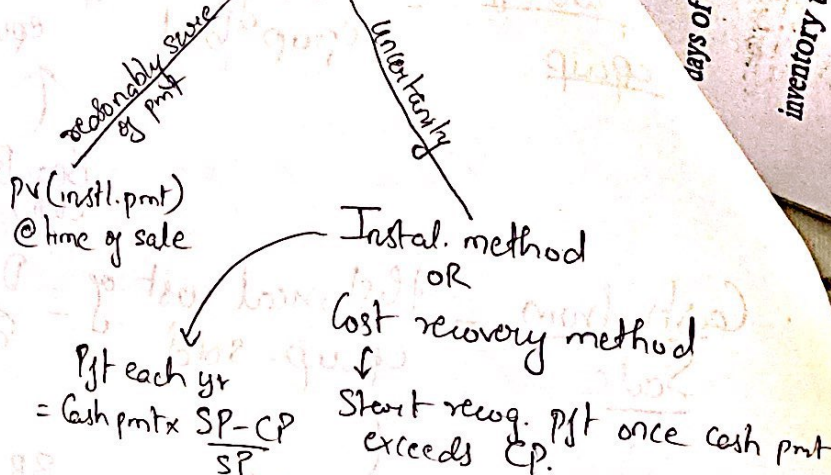
\* Income Statements

# Revenue Recognit Models

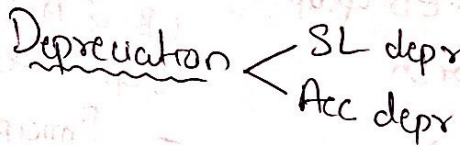
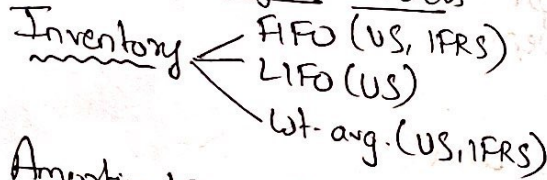
Long term contracts



Installment Sales



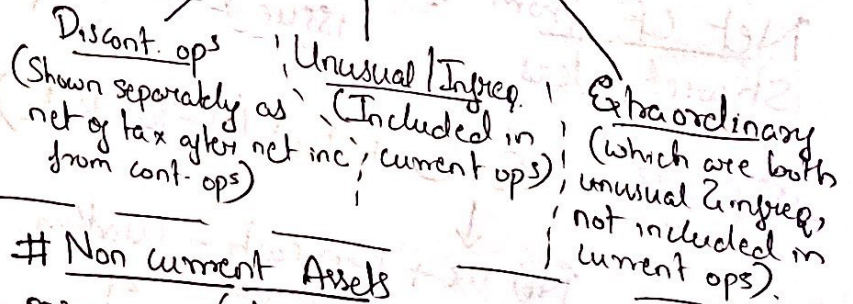
# Expense Recognit Models



Amortization

Bad debt & warranty exp. recog

Non-recurring items



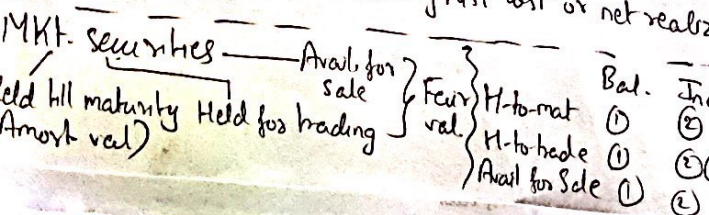
\* Balance Sheet

# Current Assets

- Cash & Cash Eq. (Amortized or Fair Val)
- MKT. securities
- Accts receivables (Net realizable acc)
- Inventories (If LIFO  $\rightarrow$  Lower of hst cost or mkt val; If not  $\rightarrow$  Lower of hst cost or net realiz. cost)

# Non current Assets

- PP&E
  - Cost Model: Amortized re hst-acc depr (IFRS & GAAP)
  - Revaluatn: Fair value - depr. (IFRS)
- Instt. property
  - Cost Model (IFRS)
  - Revaluatn Model (IFRS)
- Intangible (Research  $\rightarrow$  Expense; Development  $\rightarrow$  Capitalize)
  - Goodwill (Purchase - Fair val of A&L of acq.)
    - ① Purchased @
    - ② Int. divid, realized gain
    - ③ Unrealized



AS

sales turnover =  $\frac{\text{annual average rec}}{\text{days of sales outstanding}}$   
 inventory turn =  $\frac{\text{rec}}{\text{inventory}}$

## IFRS

$$\text{Impairment loss} = \text{Carrying val} - \text{Recoverable amt}$$

$$\text{Recoverable amt} = \max(\text{net realizable val.}, \text{PV(CF from asset)})$$

## US GAAP

Recoverability test: Impaired if carrying val > Asset's future undisc CF

$$\text{Impairment loss} = \text{Diff. btm fair val. \& carrying amt.}$$

Loss for bonds redeemed b4 maturity  
= Redemptn price - BV of bond book @ reacc. date

Bonds

debt-to-assets

financial leverage

interest coverage =